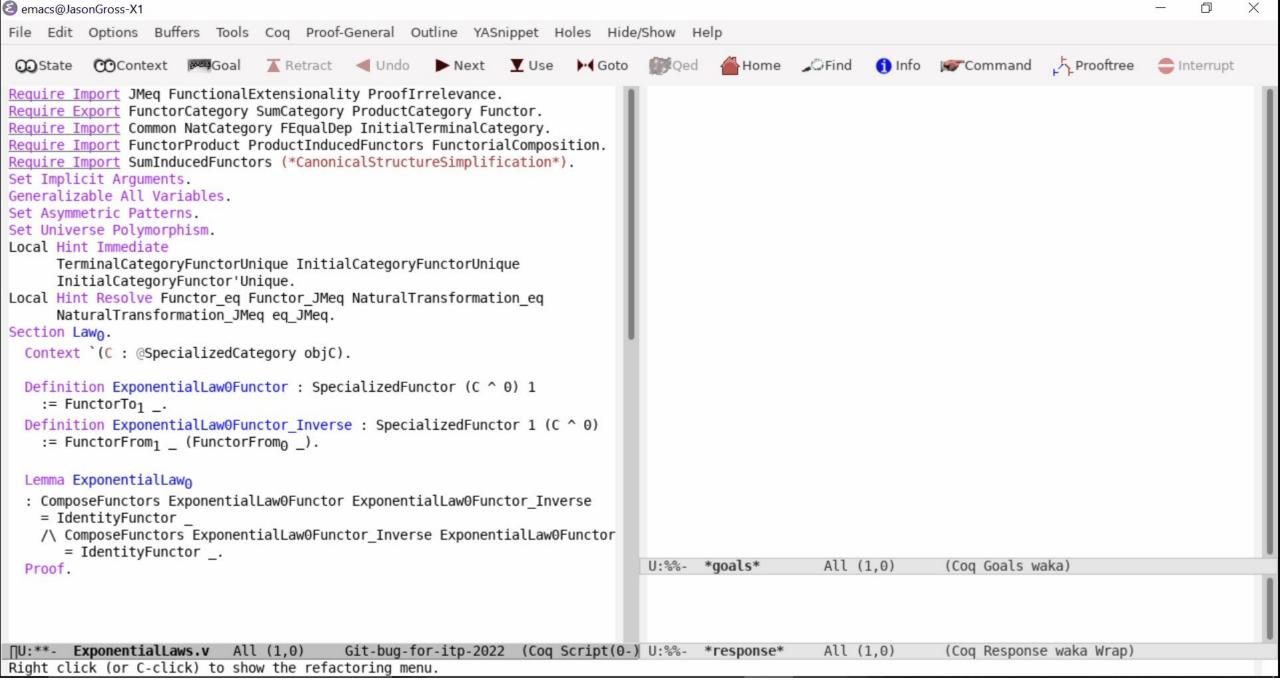
# Automatic Test-Case Reduction in Proof Assistants A Case Study in Coq

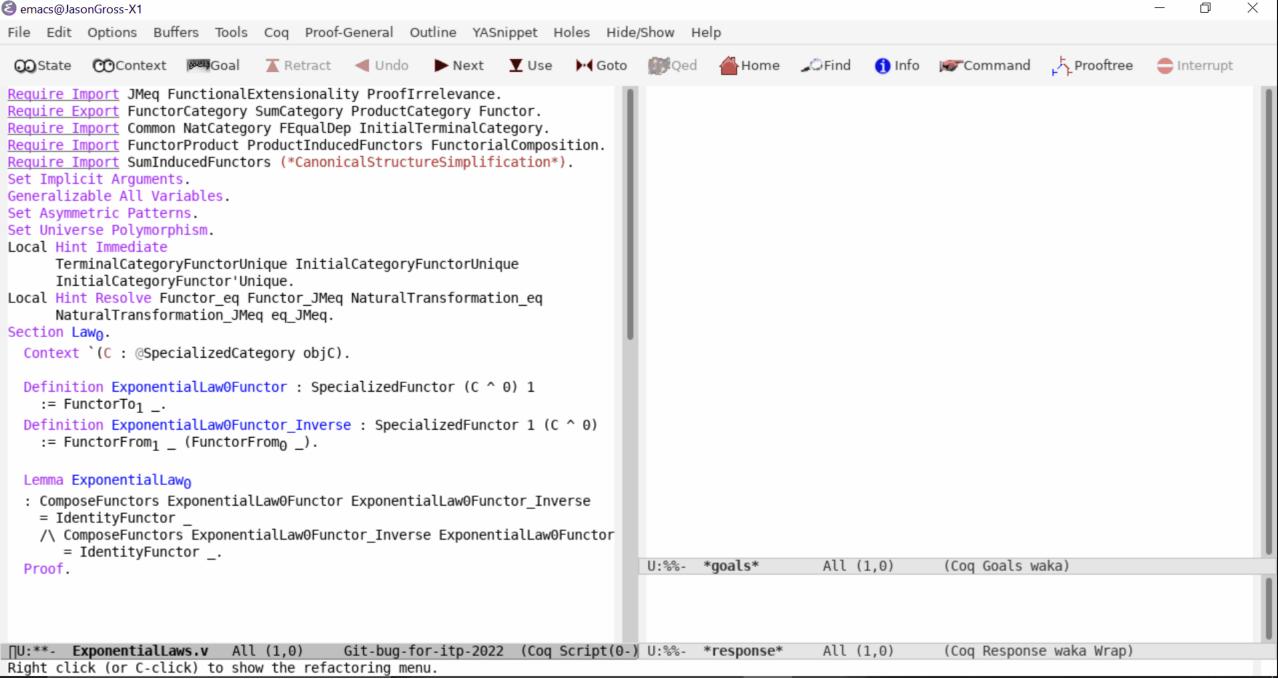
Jason Gross, Théo Zimmermann, Miraya Poddar-Agrawal, and Adam Chlipala





## Category Theory Library Minimization in Coq





split fails with `Error: Refiner was given an argument "@SpecializedFunctor (\* Set NaturalTransformation.283 Top.112 Top.113 \*) (CardinalityRepresentative O) (NatCategory (\* NaturalTransformation.283 \*) O) objC C" of type "Type (\* max(Set, Nat #7

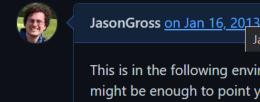
**New issue** 

<u>(</u>

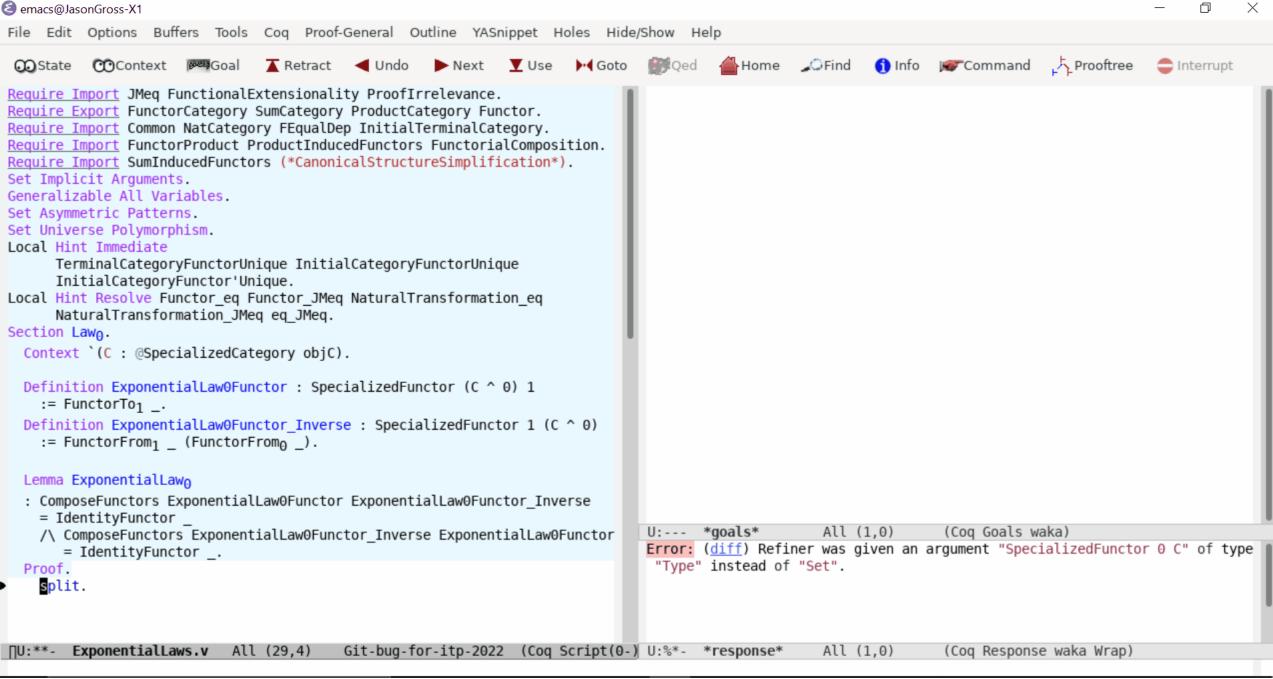
ණු

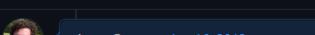
**(3)** 

Customize



```
Assignees
                                         Jan 16, 2013, 7:01 PM EST
                                                                                                                                                    No one—assign yourself
               This is in the following environment. I'll try to get a cleaner one soon, but I figured that the error message and environment
               might be enough to point you to the error
                                                                                                                                                    Labels
                                                                                                                                                    None yet
                    objC : Type (* Top.112 *)
                    C : SpecializedCategory (* Top.112 Top.113 *) objC
                    Projects
                     and
                                                                                                                                                    None yet
                           (@SpecializedFunctor (* Set Functor.290 Set Functor.290 *)
                              (CardinalityRepresentative (S 0))
                                                                                                                                                    Milestone
                             (NatCategory (* Functor.290 *) (S 0))
                             ·(CardinalityRepresentative (S 0))
                                                                                                                                                    No milestone
                              (NatCategory (* Functor.290 *) (S 0)))
                           (@ComposeFunctors (* Set Functor.290 Set Functor.290 Set
                             Functor.290 *) (CardinalityRepresentative (S 0))
                                                                                                                                                    Development
                              (NatCategory (* Functor.290 *) (S 0))
                                                                                                                                                    Create a branch for this issue or link a pull request.
                              (@SpecializedFunctor (* Set NaturalTransformation.283 Top.112
                                *Top.113 *) (CardinalityRepresentative 0)
                                 (NatCategory (* NaturalTransformation.283 *) 0) objC C)
                                                                                                                                                    Notifications
                              (@FunctorCategory (* Set NaturalTransformation.283 Top.112 Top.113
                                 Set Functor.290 *) (CardinalityRepresentative 0)
                                                                                                                                                                     \(\sigma\) Unsubscribe
                                 (NatCategory (* NaturalTransformation.283 *) 0) objC C)
https://github.com/HoTT/coq/issues/7#issue-10041042 sentative (S 0))
                                                                                                                                                    You're receiving notifications because you're watching
```







Jan 16, 2013, 7:04 PM EST

There's something odd going on here. When I have something as a goal, it fails:

```
Set Printing All.
   Goal (@eq
     (@SpecializedFunctor (CardinalityRepresentative (S O))
       (NatCategory (S 0)) (CardinalityRepresentative (S 0))
       (NatCategory (S 0)))
     (@ComposeFunctors (CardinalityRepresentative (S 0))
       (NatCategory (S 0))
       · (@SpecializedFunctor (CardinalityRepresentative O)
       (NatCategory 0) objC C)
       (@FunctorCategory (CardinalityRepresentative 0)
          (NatCategory O) objC C) (CardinalityRepresentative (S O))
       (NatCategory (S 0)) ExponentialLaw@Functor
       ExponentialLaw@Functor Inverse)
     (@IdentityFunctor (CardinalityRepresentative (S O)) (NatCategory (S O)))).
   generalize ExponentialLaw0Functor. (* Toplevel input, characters 0-33:
Error: Illegal application (Type Error):
The term "SpecializedFunctor" of type
 "forall (objC : Type) (_ : SpecializedCategory objC)
(objD : Set) ( : SpecializedCategory objD), Type"
cannot be applied to the terms
```

#### But if instead I do

```
....Set Printing All.
....Goal True.
....assert (@eq
....(@specializedFunctor (CardinalityRepresentative (S 0))
.....(NatCategory (S 0)) (CardinalityRepresentative (S 0))
.....(NatCategory (S 0)))
```

2 participants

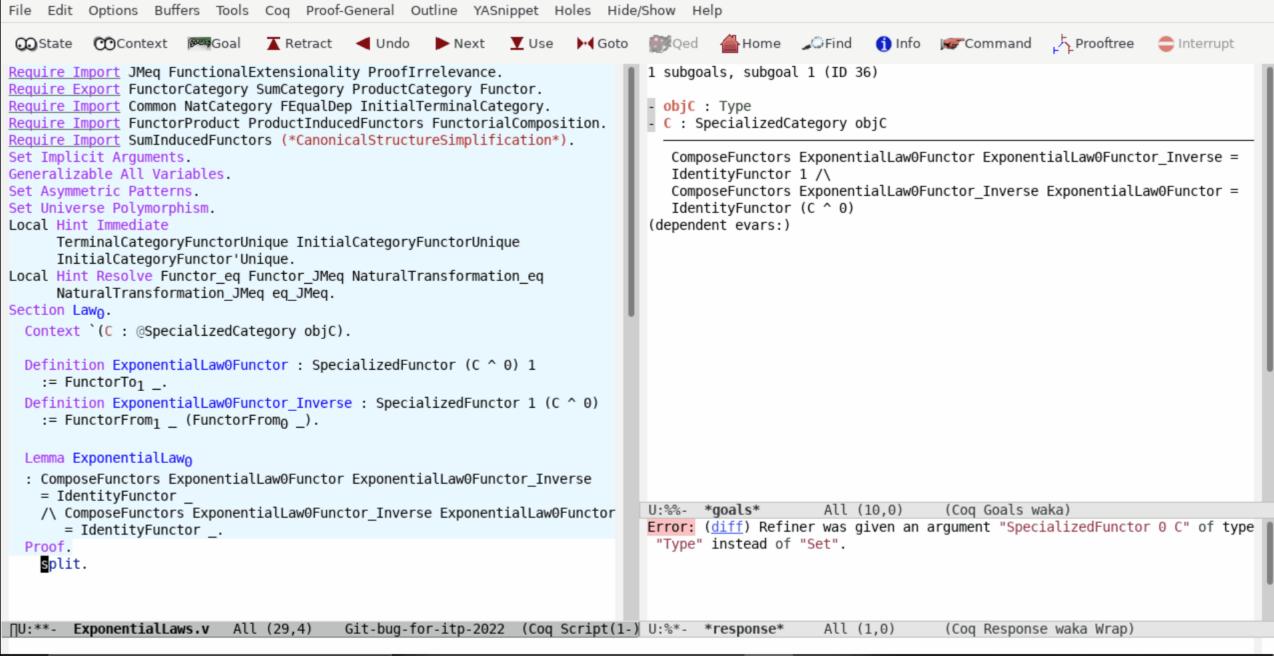


**△** Lock conversation

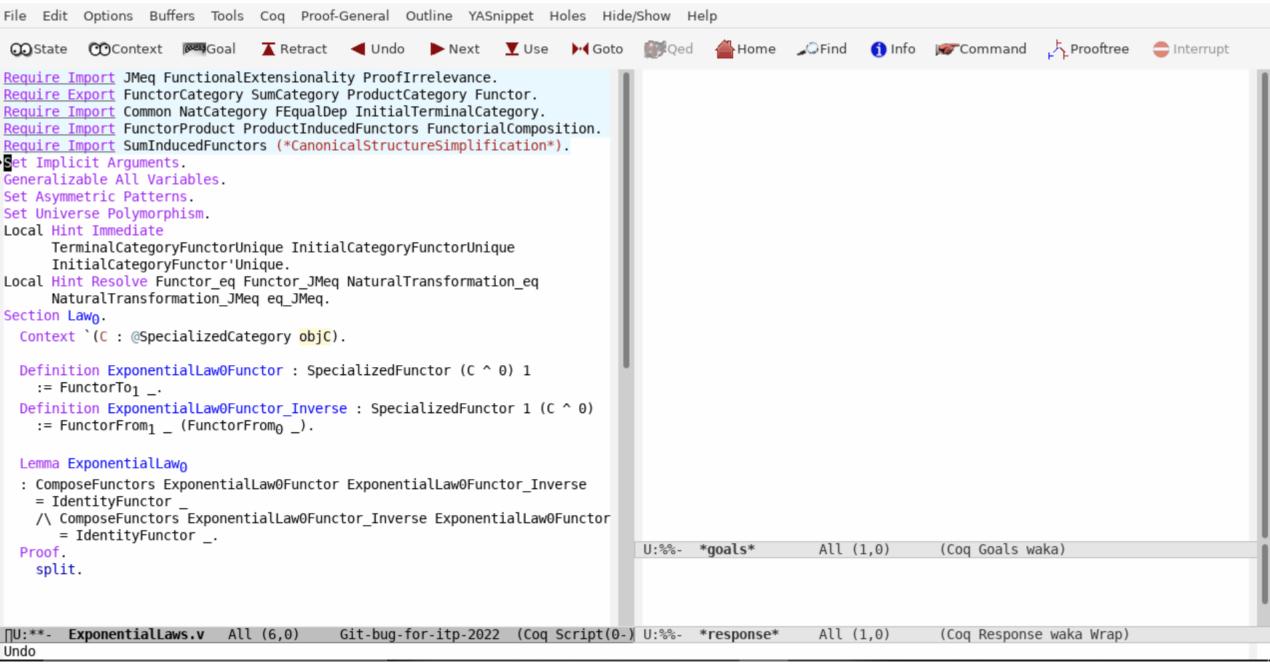
🗘 Pin issue 🗓

→ Transfer issue

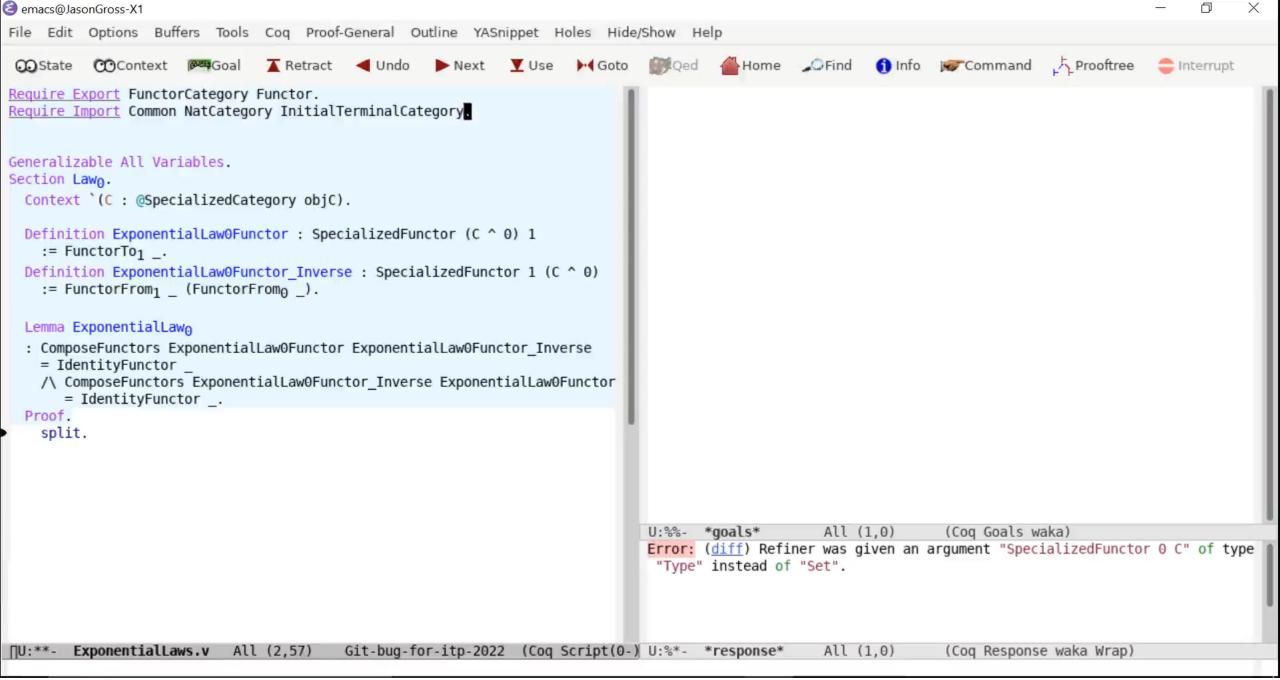
☐ Delete issue



emacs@JasonGross-X1



emacs@JasonGross-X1







#### JasonGross on Jan 16, 2013

Member Author







Jan 16, 2013, 8:01 PM EST

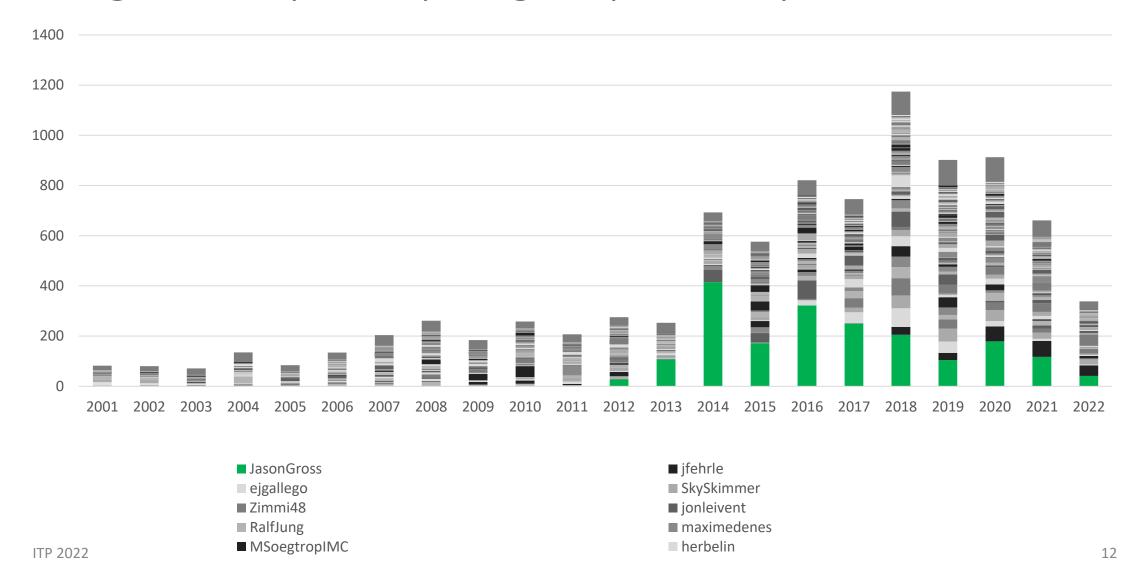
Ok, here's a self-contained version. I'm really surprised that intro can fail with Illegal application (Type Error) I'll try to trim this down sometime soon, but, if I don't get to it, I hope it's enough to work off of:

```
Delimit Scope object scope with object.
Delimit Scope morphism scope with morphism.
Delimit Scope category scope with category.
Delimit Scope functor scope with functor.
Set Implicit Arguments.
Generalizable All Variables.
Polymorphic Record SpecializedCategory (obj : Type) := Build_SpecializedCategory' {
  Object :> _ := obj;
 Morphism' : obj -> obj -> Type;
  ·Identity' : forall o, Morphism' o o;
  ·Compose' : forall s d d', Morphism' d d' -> Morphism' s d -> Morphism' s d';
  Associativity' : forall o1 o2 o3 o4 (m1 : Morphism' o1 o2) (m2 : Morphism' o2 o3) (m3 : Morphism' o3 o4),
    Compose' (Compose' m3 m2) m1 = Compose' m3 (Compose' m2 m1);
  (* ask for [eq_sym (Associativity' ...)], so that C^{op}^{op} is convertible with C *)
```

It has something to do with the intros; autorewrite with functor; reflexivity line; if I change that to admit, it all goes through. (Same thing if I do the rewriting manually.)



#### Origin Story: Coq Bug Reports By Year



Goal: Automate This!

14

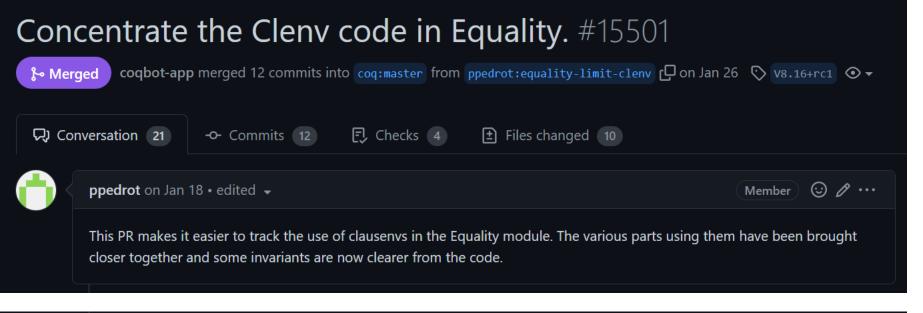
Every 0.1s: ./watch.sh head -70

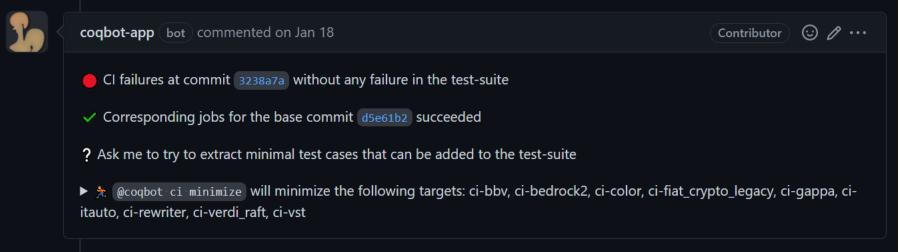
ITP 2022

cat: bug\_01.v: No such file or directory

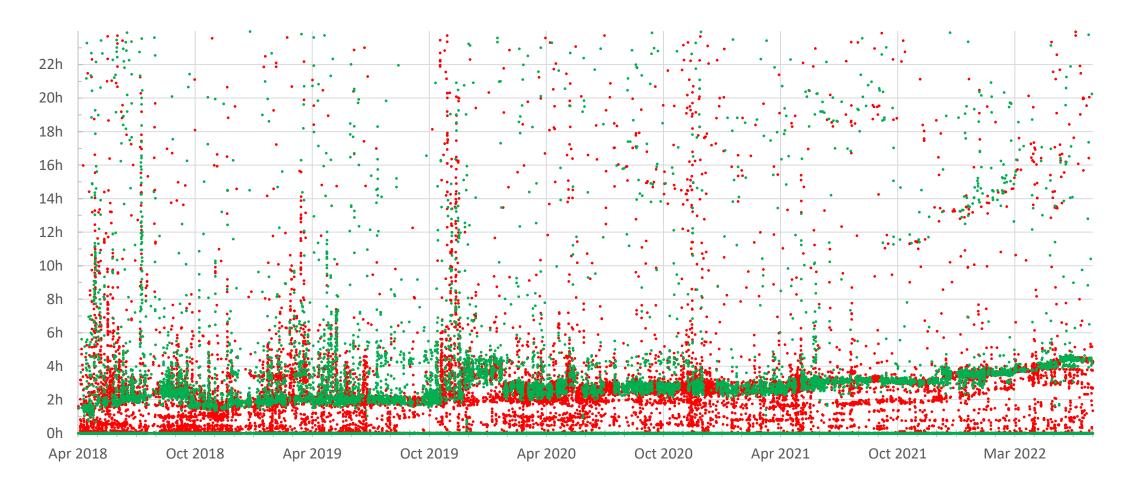
🎍 jgross@JasonGross-X1: ~/catd 🗴 🕂 🗸 X jgross@JasonGross-X1:-/catdb\$ command time -f "(real: %e, user: %U, sys: %S, mem: %M ko)" find-bug.py ExponentialLaws.v bug\_01.v -R . "" --no-deps --coqbin=../HoTT-coq/bin/

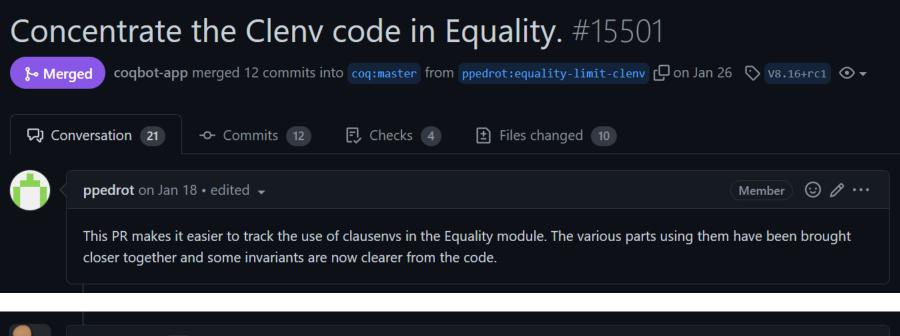
## Debugging Regressions: coqdev experience

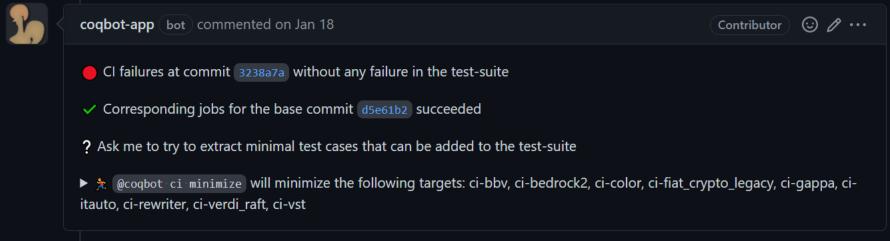


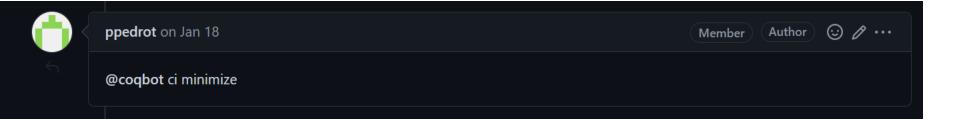


## CI Running Time











ppedrot on Jan 18

Member Author





@coqbot ci minimize



cogbot-app (bot) commented on Jan 18

Contributor © / ...

I have initiated minimization at commit 3238a7a for the suggested targets ci-bbv, ci-bedrock2, ci-color, ci-fiat\_crypto\_legacy, ci-gappa, ci-itauto, ci-rewriter, ci-verdi\_raft, ci-vst as requested.



coqbot-app (bot) commented on Jan 18

Contributor 😉 🧷 · · ·

Minimized File /github/workspace/builds/coq/coq-failing/\_build\_ci/bbv/src/bbv/Word.v (from ci-bbv) (full log on GitHub Actions)

We are collecting data on the user experience of the Coq Bug Minimizer. If you haven't already filled the survey *for this PR*, please fill out our short survey!

- ► Minimized Coq File (consider adding this file to the test-suite)
- ► Intermediate Coq File (useful for debugging if minimization did not go as far as you wanted)
- ▶ Build Log (contains the Coq error message) (truncated to last 8.0KiB; full 2.7MiB file on GitHub Actions Artifacts under build.log )
- ▶ Minimization Log (truncated to last 8.0KiB; full 82KiB file on GitHub Actions Artifacts under bug.log)

If you have any comments on your experience of the minimizer, please share them in a reply (possibly tagging @JasonGross). If you believe there's a bug in the bug minimizer, please report it on the bug minimizer issue tracker.





Minimized File /github/workspace/builds/coq/coq-failing/\_build\_ci/bbv/src/bbv/Word.v (from ci-bbv) (full log on GitHub Actions)

We are collecting data on the user experience of the Coq Bug Minimizer.

If you haven't already filled the survey *for this PR*, please fill out our short survey!

▼ Minimized Coq File (consider adding this file to the test-suite)

```
(* -*- mode: coq; coq-prog-args: ("-emacs" "-q" "-w" "-deprecated-native-compiler-option" "-Q" "/github/workspace/cwd"
(* File reduced by coq-bug-minimizer from original input, then from 7591 lines to 50 lines, then from 55 lines to 49 l
(* cogc version 8.16+alpha compiled with OCaml 4.05.0
  coqtop version runner-zxwgkjap-project-6138686-concurrent-0:/builds/coq/coq/ build/default,(HEAD detached at e1c1bcc
Set Implicit Arguments.
Inductive word : nat -> Set :=
| WO : word O
| WS : bool -> forall n, word n -> word (S n).
Fixpoint wones (sz : nat) : word sz.
Admitted.
Definition whd sz (w : word (S sz)) : bool.
Admitted.
Definition wtl sz (w : word (S sz)) : word sz.
Admitted.
Fixpoint combine (sz1 : nat) (w : word sz1) : forall sz2, word sz2 -> word (sz1 + sz2) :=
 match w in word sz1 return forall sz2, word sz2 -> word (sz1 + sz2) with
····| WO => fun w' => w'
.... | WS b w' => fun w'' => WS b (combine w' w'')
 end.
Fixpoint split1 (sz1 sz2 : nat) : word (sz1 + sz2) -> word sz1.
Admitted.
Fixpoint wnot sz (w : word sz) : word sz :=
  match w with
· · · · | WO => WO
   \cdot | WS h w' => WS (negh h) (what w')
```

```
match w with
---- WO => WO
····| WS b w' => WS (negb b) (wnot w')
  end.
Fixpoint bitwp (f : bool -> bool -> bool) sz (w1 : word sz) : word sz -> word sz :=
  match w1 with
····| WO => fun => WO
.... | WS b w1' => fun w2 => WS (f b (whd w2)) (bitwp f w1' (wtl w2))
  end.
Definition wnot' sz := bitwp xorb (wones sz).
Theorem split1 combine : forall sz1 sz2 (w : word sz1) (z : word sz2),
 split1 sz1 sz2 (combine w z) = w.
Admitted.
Theorem wnot_wnot'_equiv : forall sz (w : word sz), wnot w = wnot' w.
Admitted.
Theorem wnot split1 : forall sz1 sz2 w, wnot (split1 sz1 sz2 w) = split1 sz1 sz2 (wnot w).
Proof.
  intros.
  repeat rewrite wnot_wnot'_equiv.
  unfold wnot'.
  'erewrite <- split1_combine with (w':= wones _).</pre>
```

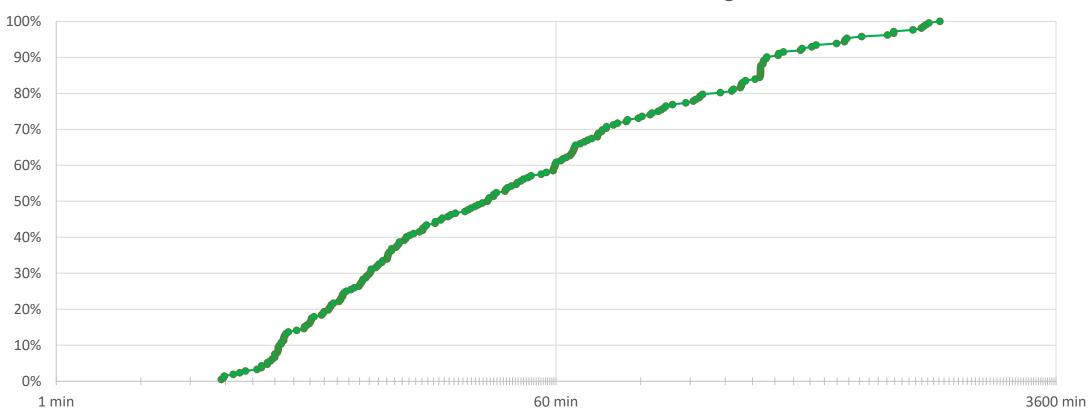
- ► Intermediate Cog File (useful for debugging if minimization did not go as far as you wanted)
- ▶ Build Log (contains the Coq error message) (truncated to last 8.0KiB; full 2.7MiB file on GitHub Actions Artifacts under build.log)
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If you have any comments on your experience of the minimizer, please share them in a reply (possibly tagging @JasonGross). If you believe there's a bug in the bug minimizer, please report it on the bug minimizer issue tracker.

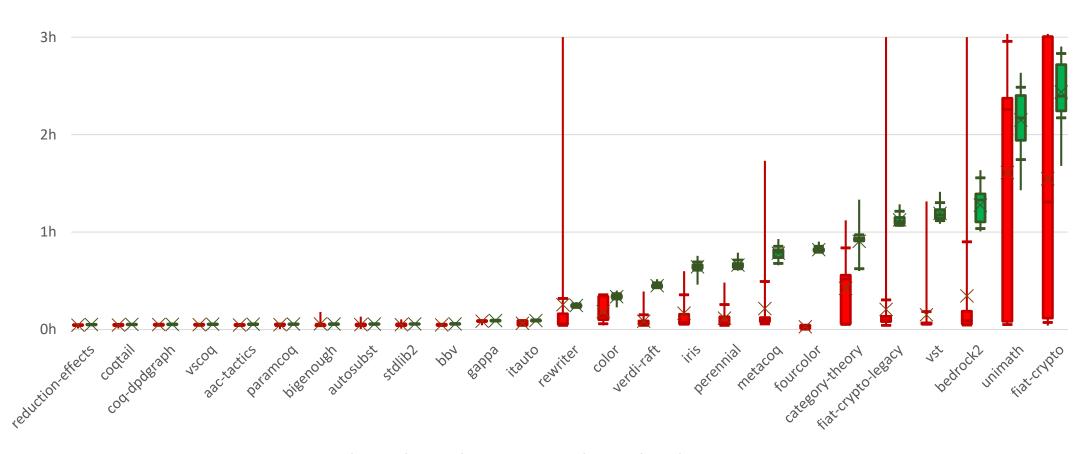
## How Long Does It Take?

## Minimizer Running Time CDF

#### % of Minimizer Runs vs Maximum Running Time

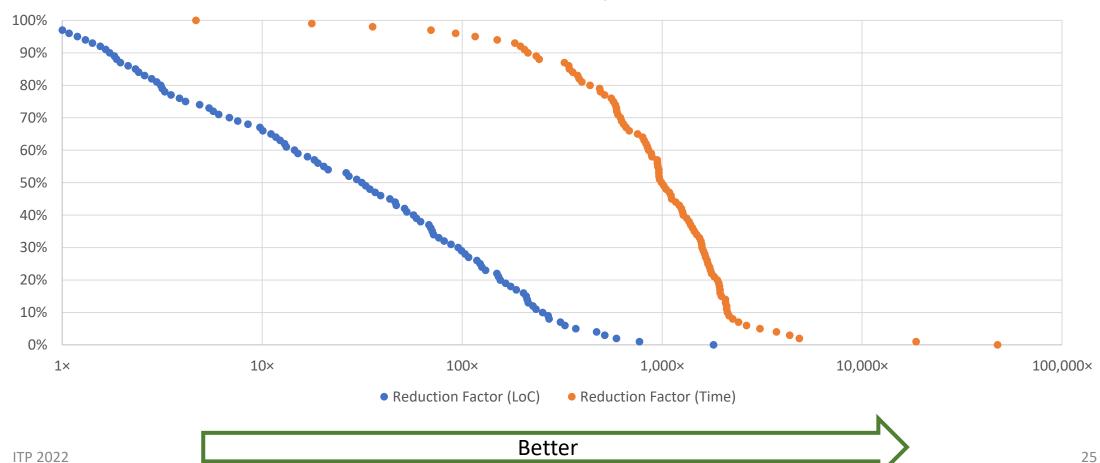


## How Long Do Projects Take On CI?

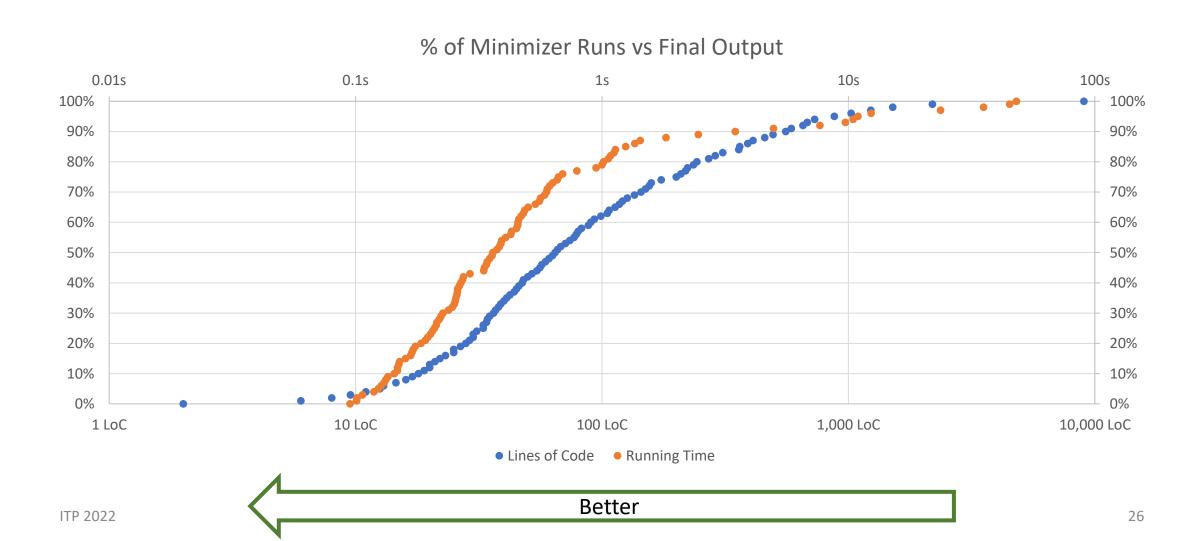


#### How Much Do We Minimize?





#### How Minimal is Minimal in Absolute Terms?



## Specification Summary

- Input: a development displaying a potential problem with Coq
- Output: a single (shorter, faster) file displaying the same behavior
- Desires:
  - File should be standalone, as short as possible, as fast as possible
  - Fully automated, no interaction beyond pointing it at the issue initially
  - Interruptible and resumable: user should be able to do a manual pass over the file at any point and resume automatic minimization from there

## Specification Details

What does "the same behavior" mean?

- In bug reporting case: "same" error message, without changing the final bit of code
  - "print 'exact error message'" is not a valid minimization
- In CI case: should also succeed on the master version of Coq

#### What needs to be automated?

- Workflow automation (responding to user's comment, replying as a comment)
- Removing code to shorten example (in compile time and LoC)
- Adjustments to minimize compile time
- Inlining and linearization (to reduce complexity)

#### How do we do this?

- Interfacing with Coq externally
- Delta debugging / brute force
- Tricks for inlining

#### To Achieve Adequate Performance:

- Inline files one-by-one
- Remove proof scripts as early as possible
- Linear pass to remove code, don't consider all subsets

#### Delta Debugging / Brute Force Removal

- "Trust me, it's true" primitives
- Not line by line, but blocks
- Minimal coupling, lack of forward references

```
Coupling in Agda:
data \mathbb{N}: Set where
  zero: N
  SUCC : \mathbb{N} \to \mathbb{N}
data Even : N → Set
data Odd : N → Set
data Even where
  even-zero : Even zero
  even-succ : \forall {n} \rightarrow Odd n \rightarrow Even (succ n)
data Odd where
  odd-succ : \forall {n} \rightarrow Even n \rightarrow Odd (succ n)
```

#### Coupling in Agda:

data  $\mathbb{N}$  : Set where

zero: N

 $succ : \mathbb{N} \to \mathbb{N}$ 

data Even : N → Set

data Odd : N → Set

data Even where

even-zero: Even zero

even-succ :  $\forall$  {n}  $\rightarrow$  Odd n  $\rightarrow$  Even (succ n)

#### data Odd where

odd-succ :  $\forall$  {n}  $\rightarrow$  Even n  $\rightarrow$  Odd (succ n)

**Wbsimgdype**: signature for data definition Even

**Whetoskowpingharking** the declared ibut not accompanied by a definition: Execution when scope checking Odd



#### Coupling in Agda:

data  $\mathbb{N}$  : Set where

zero : №

 $succ : \mathbb{N} \to \mathbb{N}$ 



Coupled definitions are almost always single statements in Coq

```
Inductive N : Set :=
| zero : N |
| succ : N -> N.
Inductive Even : N -> Set :=
| even_zero : Even zero
| even_succ : forall {n}, Odd n -> Even (succ n)
with Odd : N -> Set :=
| odd_succ : forall {n}, Even n -> Odd (succ n).
```

#### How do we do this?

- Interfacing with Coq externally
- Delta debugging / brute force
- Tricks for inlining

## Tricks for Inlining and Linearization

## Name Changes on Inlining

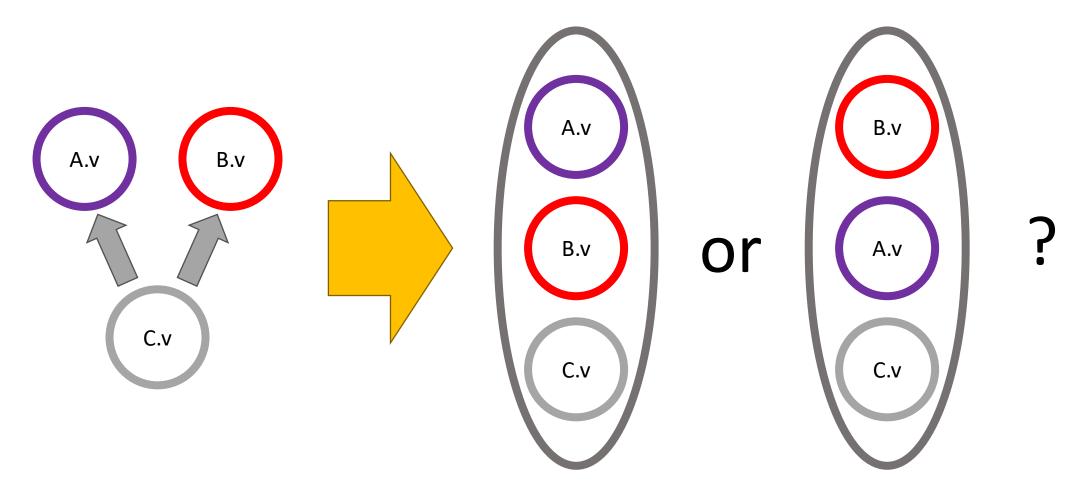
```
A.v:
Definition foo
: nat := 0.
B.v:
Require Import A.
Definition foo
: nat := 1.
Print foo.
(*foo = 1 : nat*)
Print A.foo.
(*A.foo = 0 : nat*)
```

```
Definition foo
: nat := 0.
Definition foo
: nat := 1.
(* Error: foo
already exists. *)
Print foo.
(*foo = 1 : nat*)
Print A.foo.
```

VS

```
Module A.
Definition foo
: nat := 0.
End A.
Import A.
Definition foo
: nat := 1.
Print foo.
(*foo = 1 : nat*)
Print A.foo.
(*A.foo = 0 : nat*)
```

#### Linearization



## How to make your proof assistant amenable to minimization

- Make it possible to have a single file with the same semantics as code in multiple files
- Primitive for "trust me, it's true"
- Lack of forward references is nice

Don't forget the last mile of automating integration with CI!

#### Future Work

- More automation of bug reporter work flow
- Better inlining
- More minimization
- Other proof assistants???

#### Extra Content

#### How Long Do Projects Take On CI?

